What is topology?

Jon Woolf

February, 2010

Set of tube stations

A
Acton Town
Aldgate
Aldgate East
Alperton
Amersham
Angel
Archway
Arnos Grove
Arsenal
B
Baker Street
Balham
Bank
Barbican
Barking
Barkingside
Barons Court
Bayswater
Becontree
Belsize Park
Bermondsey
Bethnal Green
Blackhorse Road
Blackfriars
Bond Street
Borough
Boston Manor
Bounds Green
Bow Church
Bow Road
Brent Cross
Brixton
Bromley-by-Bow
Buckhurst Hill
Burnt Oak
C
Caledonian Road
Camden Town
Canada Water
Canary Wharf
Canning Town

H
Hanwell
Hammersmith
Hampstead
Hanger Lane
Harlesden
Harrow-on-the-Hill
Hatton Cross
Heathrow
Hendon Central
High Barnet
High Street Kensington
Highbury & Islington
Highgate
Hillingdon
Holborn
Holland Park
Holloway Road
Hornchurch
Hounslow Central
Hounslow East
Hounslow West
Hyde Park Corner
I
Ickenham
K
Kennington
Kensal Green
Kensington (Olympia)
Kentish Town
Kenton
Kew Gardens
Kilburn
Kilburn Park
Kings Cross St. Pancras
Knightsbridge
L
Ladbroke Grove
Lambeth North
Lancaster Gate
Latimer Road

R
Ravenscourt Park
Rayners Lane
Redbridge
Regents Park
Richmond
Rickmansworth
Roding Valley
Rotherhithe
Royal Albert
Royal Oak
Royal Victoria
Ruislip
Ruislip Gardens
Ruislip Manor
Russell Square
S
Seven Sisters
Shadwell
Shepherds Bush
Shoreditch
Snaresbrook
South Ealing
South Harrow
South Kensington
South Kenton
South Quay
South Ruislip
South Wimbledon
South Woodford
Southfields
Southgate
Southwark
St. James's Park
St. John's Wood
St. Paul's
Stamford Brook
Stanmore
Stepney Green
Stockwell
Stonebridge Park
Stratford

Cannon Street
Canons Park
Chalfont & Latimer
Chalk Farm
Chancery Lane
Charing Cross
Chesham
Chigwell
Chiswick Park
Chorleywood
Clapham Common
Clapham North
Clapham South
Cockfosters
Colindale
Colliers Wood
Covent Garden
Croxley
D
Dagenham East
Dagenham Heathway
Debden
Devons Road
E
Ealing Broadway
Ealing Common
Earls Court
East Acton
East Finchley
East India
East Putney
Eastcote
Edgware
Edgware Road
Elephant & Castle
Elm Park
Embankment
Epping
Euston
Euston Square
F
Farringdon

Leicester Square
Leyton
Leytonstone
Limehouse
Liverpool Street
London Bridge
London Road
M
Maida Vale
Manor House
Mansion House
Marble Arch
Marylebone
Mile End
Mill Hill East
Monument
Moor Park
Moorgate
Morden
Mornington Crescent
Mudchute
N
Neasden
New Cross
New Cross Gate
Newbury Park
North Acton
North Ealing
North Greenwich
North Harrow
North Wembley
Northolt
Northwick
Northwood
Northwood Hills
Notting Hill Gate
O
Oakwood
Old Street
Osterley
Oval
Oxford Circus
P

Sudbury Hill
Sudbury Town
Surrey Quays
Swiss Cottage
T
Temple
Theydon Bois
Tooting Bec
Tooting Broadway
Tottenham Court Rd
Tottenham Hale
Totteridge & Whetstone
Tower Gateway
Tower Hill
Tufnell Park
Turnham Green
Turnpike Lane
U
Upminster Bridge
Upney
Upton Park
Uxbridge
V
Vauxhall
Victoria
W
Walthamstow Central
Wanstead
Wapping
Warren Street
Warwick Avenue
Waterloo
Watford
Wembley Central
Wembley Park
West Acton
West Brompton
West Finchley
West Ham
West Hampstead
West Harrow
West India Quay
West Kensington
West Ruislip

Finchley Central
Finchley Road
Finsbury Park
Fulham Broadway
G
Gants Hill
Gloucester Road
Golders Green
Goldhawk Road
Gospel Oak
Granary Hill
Great Portland St
Green Park
Greenford
Gunnersbury

Paddington
Park Royal
Parsons Green
Perivale
Piccadilly Circus
Pimlico
Pinner
Plaistow
Poplar
Preston Road
Prince Regent
Pudding Mill Lane
Putney Bridge
Q
Queens Park
Queensbury
Queensway

Westbourne Park
Westferry
Westminster
White City
Whitechapel
Willesden Junction
Wimbledon
Wimbledon Park
Wood Green
Woodford
Woodside Park

Geometric map of the tube

Topological map of the tube
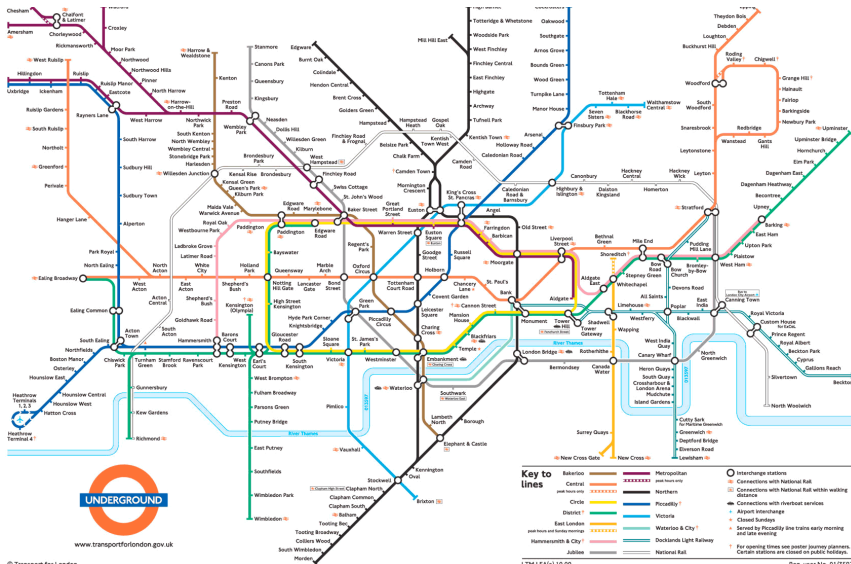
Spaces from sets with relations

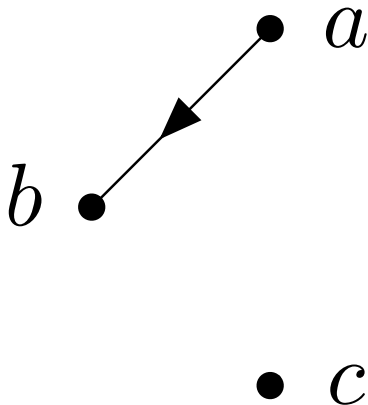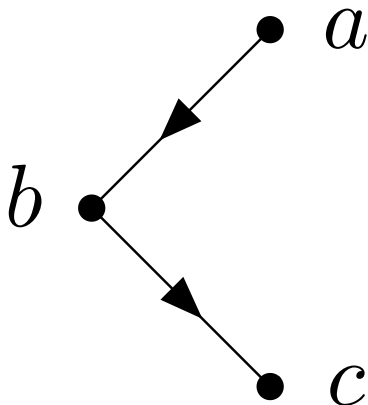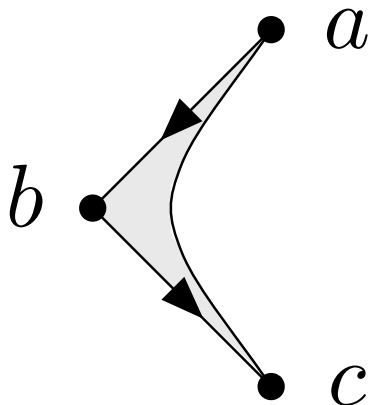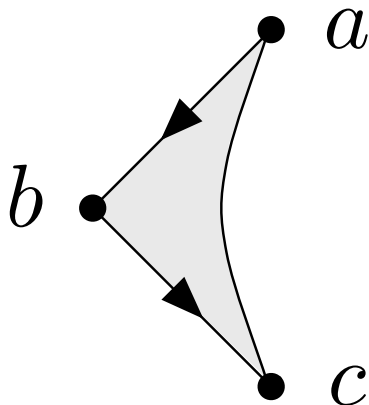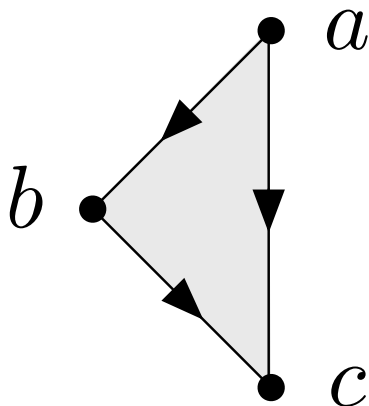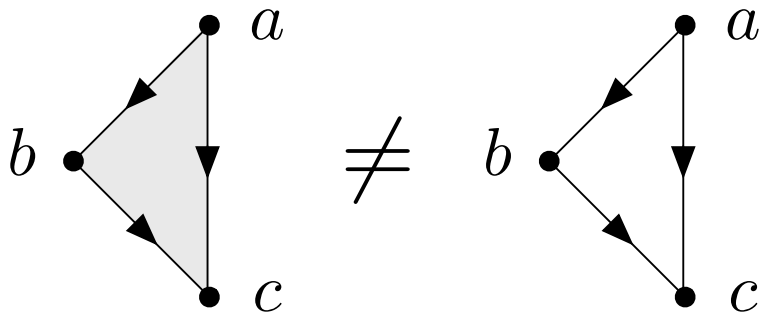# Spaces from sets with relations

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In a sense, all spaces arise in this way.

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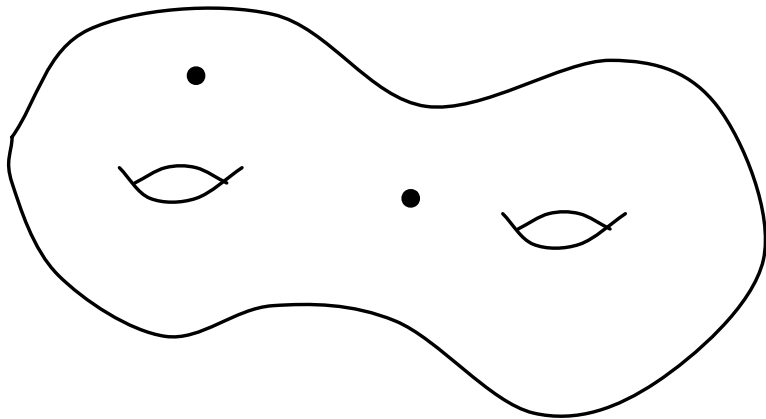
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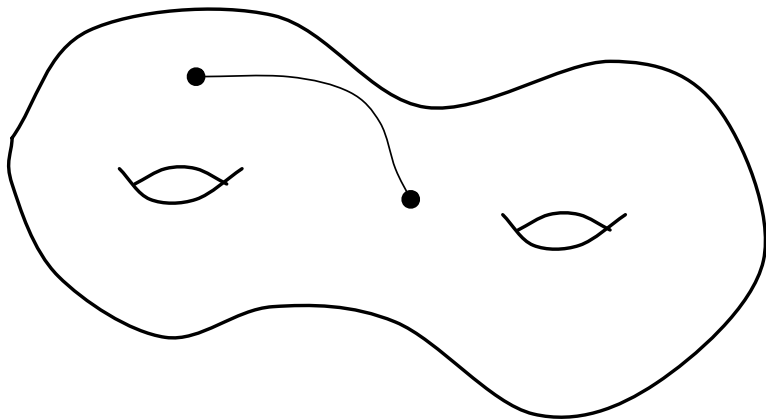
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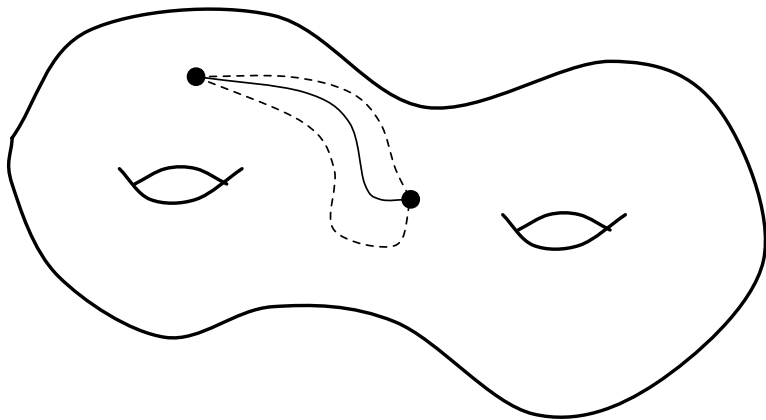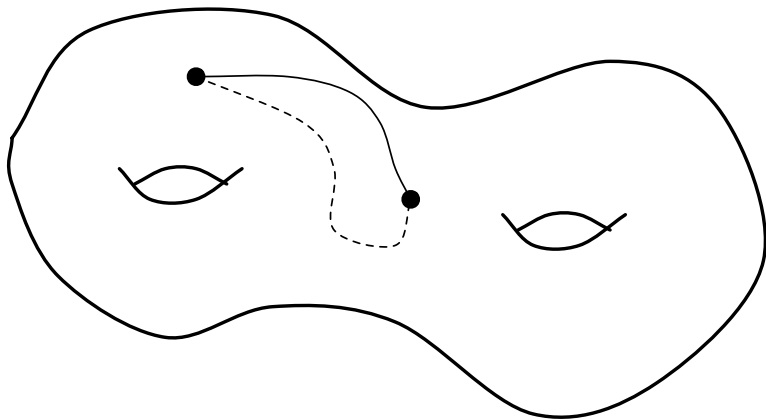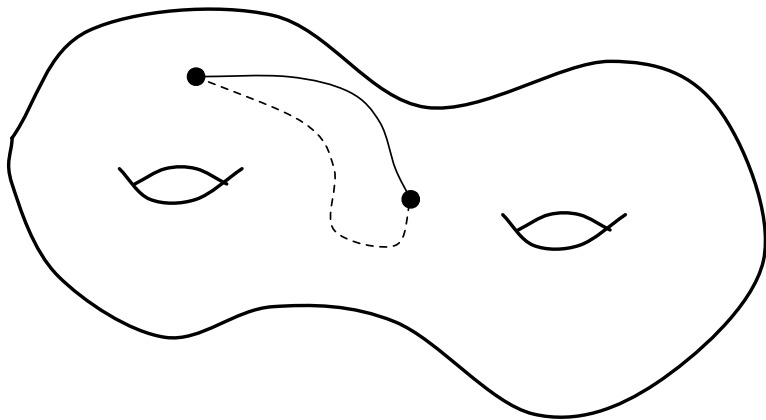
Homotopy theory

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