Assignment 10 Deadline = Tuesday of Week 11

Please submit written solutions in lectures, and email me your Maple file, 'assignment10<name>.mw', by Tuesday of Week 11.

Q1. Solve the initial value problem, with h = 0.125,

$$\frac{dy}{dx} = ye^{-3x} - y^2,$$
 $y(0) = 1$

using both the explicit and implicit Euler method to find y(0.25). Compare the two absolute errors, taking y(0.25) = 0.9342 as the exact value. Check your answer with Maple. How does the error in the explicit method depend on the choice of h? To test this, decrease h in the maple file. For example, try dividing h by 2 and by 4, and see how the error varies with h.

Q2. Solve the initial value problem, with h = 0.2,

$$\frac{dx}{dt} = -20(x-t) + 1, \qquad x(0) = 2$$

using both the explicit and implicit Euler method to find x(0.4). Compare the two absolute errors, given that the exact solution is $x(t) = t + 2e^{-20t}$. Which method is better? Why?

Q3. Solve the initial value problem, with h = 0.1,

$$\frac{dy}{dx} = \sin y + x, \qquad \qquad y(0) = 1$$

using the implicit Euler method combined with the Newton-Raphson method (take no more than 3 steps of the N-R method at each step of the implicit Euler method) to calculate y(0.2). Check your answer with Maple.